

Hybrid Differential Evolution and Particle Swarm Optimization Algorithm for the Sugarcane Cultivation Scheduling Problem

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ABSTRACT

This paper focuses on optimizing scheduling solutions for the flexible flow shop problem, with tooling constraints and machine eligibility, to minimize makespan for cultivating sugarcane. Normally, preparing the soil for planting sugarcane requires six steps: 1) 7 power harrow and rototiller, 2) rotary mini combine, 3) 22/24 disc harrow, 4) rotary mini combine, 5) sugarcane plantation, and 6) sugarcane sprayer. Each of these steps requires a variety of tools. With limited availability of tools and equipment, resource allocation is important. The objective of this research was to minimize the makespan. For optimal convergence, meta-heuristics, such as a Differential Evolution algorithm, a Particle Swarm optimization algorithm, and a Hybrid DEPSO algorithm were developed to solve the problem. Experimental results showed that all three methods efficiently solved flexible flow shop problems.

Keywords: Scheduling, Tool limitations, Tooling constraints, Tool change, Differential evolution, Particle swarm optimization, Sugarcane

INTRODUCTION

Sugarcane is an important crop in Thailand, the second largest sugar exporter in the world (Office of the Cane and Sugar Board, 2016). Increasing demand for cultivating sugarcane in Thailand has outstripped resources, especially for small farmers who do not own their own agricultural machinery. Preparing the fields for planting requires hiring large and expensive operators (Prasara and Gheewala, 2016). Thus, better allocation of resources is important to reduce the cost of producing sugarcane (Sugar Research Australia, 2017).

Preparing the soil for sugarcane production involves six steps, denoted here by the principal tool required: 1) 7 power harrow and rototiller, 2) rotary mini combine, 3) 22/24 disc harrow, 4) rotary mini combine, 5) sugarcane plantation, and 6) sugarcane sprayer. Steps 1, 4, 5, and 6 require small tractors and Steps 2 and 3 require medium- to large-sized tractors (see Figure 1). This study attempts to find solutions to the scheduling challenges inherent in

sugarcane cultivation created by these resource/machinery constraints, with the objective of minimizing completion time. The constraints include flexible flow shop, the need for the same machine at multiple steps, and limited tools.

Many researchers have presented a variety of flexible flow shop models based on the traditional flexible flow shop scheduling problem. The flexible flow shop problem is an NP-hard problem, and metaheuristic algorithms have been presented as the most optimal way to handle such large problems (Hoogeveen et al., 1996; Gupta et al., 2002; Wang and Hunsucker, 2003; Baumann and Trautmann, 2011). Many algorithms have been designed to help solve these problems, including tabu search algorithms (Widmer, 1991), hybridization of particle swarm optimization with Cauchy distribution for optimal sequences (Sangsawang et al., 2015), a modified genetic algorithm for hybridized ant colony optimization (Chamnanlor et al., 2017), and a simulated annealing based heuristic (Batur et al., 2016). Flexible flow shop problems are complex. Several applied mathematical models and metaheuristics have been developed as solutions, such as those by Melnyk et al. (1989), Widmer (1991), Ghosh et al. (1992), Gultekin et al. (2006), Chen (2008), Zhonghua et al. (2009), Zeballos (2010), Zeballos et al. (2010), Xu et al. (2013), and Özpeynirci et al. (2016). Recent research has applied evolutionary computing methods. Differential evolution is one of the strongest methods for continuous optimization, with an algorithm that has been successfully applied with several techniques. For example, Zhou (2012) used the new differential evolution algorithm based on a variable neighborhood search to contribute toward solving the flow shop scheduling problem. Tonge and Kulkarni (2013) improved the differential evolution algorithm using the classical Nawaz Ensore Ham algorithm and iterated local search, with an enhanced swap operator to minimize makespan. Many researchers have used differential evolution algorithms to minimize makespan (Rahman et al., 2014; Moonsri et al., 2015; Santosa and Riyanto, 2016). The particle swarm optimization algorithm is another interesting method (Liang et al., 2006; Nasir et al., 2012). This technique was first proposed by Eberhart and Kennedy (1995) and provides simple instrumentality that has been successfully employed in many areas of research. Additionally, much research on the particle swarm optimization algorithm has focused on diversifying the search to prevent premature convergence and allow the algorithm to escape from local minima (Shi and Eberhart, 1998; Yang and Simon, 2005). Currently, the literature combines particle swarm optimization and iterated local search to solve hybrid flow shop scheduling problems with preventive maintenance activities (Li et al., 2014). To increase performance and alleviate the defects of problem solving, the hybrid DEPSO algorithm has been proposed (Jayabarathi, 2007; Li et al., 2008; Pant et al., 2008).

This paper proposes a solution that applies differential evolution, particle swarm optimization, and hybrid DEPSO to the problem of tractor scheduling, with the objective of minimizing the makespan. The results from this study can serve as a prototype for developing decision tools for sugarcane cultivation and can also be applied to other industrial crops.

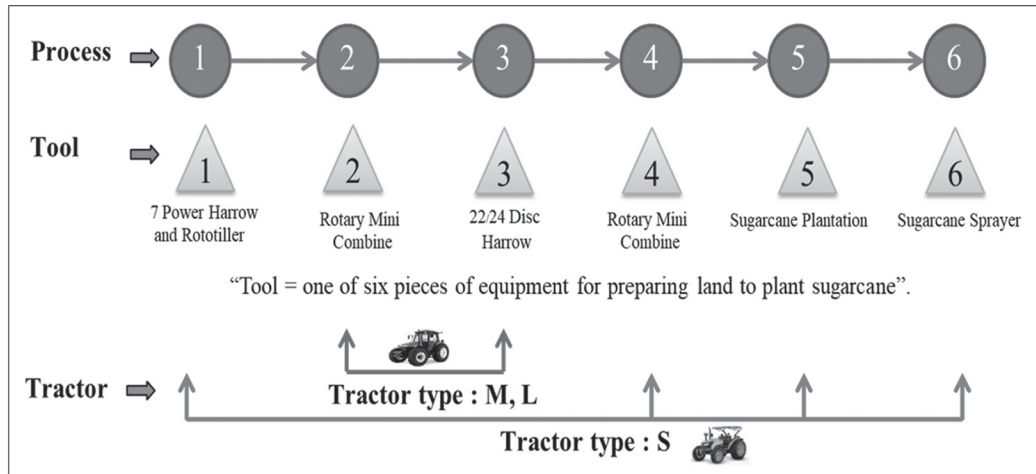


Figure 1. Characteristics of the problem.

MATERIALS AND METHODS

Differential evolution algorithm

Storn and Price (1997) developed the differential evolution algorithm for continuous optimization problems:

Notation:

- G : Generation number
- P_G : Population of NP-D-dimension
- $X_{i,G}$: Random vector
- $V_{i,G}$: Mutant vector
- $U_{i,G}$: Trial vector
- D : Dimensional parameter
- $\text{randb}(j)$: A random number generated from $[0,1]$
- $\text{rnbr}(i)$: A random integer from $[1, 2, \dots, D]$
- J_{rand} : Position vector of particle i
- F : Scaling factor

Differential evolution:

Step 1: Set the generation number $G = 0$, $P_G = \{X_{1,G}, \dots, X_{NP}\}$ with $X_{i,G} = \{x_{i,G}^1, \dots, x_{i,G}^D\}$, $i = 1, \dots, NP$, uniformly distributed in the range $[X_{\min}, X_{\max}]$, where $X_{\min} = \{x_{\min}^1, \dots, x_{\min}^D\}$ and $X_{\max} = \{x_{\max}^1, \dots, x_{\max}^D\}$.

Step 2: WHILE stopping criterion is not satisfied, DO

Step 2.1: Mutation

/*Generate a mutated vector $V_{i,G} = \{v_{i,G}^1, \dots, v_{i,G}^D\}$ for each target vector $X_{i,G}$ */

FOR i=1 to NP

Generate a mutated vector $V_{i,G} = \{v_{i,G}^1, \dots, v_{i,G}^D\}$ corresponding to the target vector $X_{i,G}$

END FOR

Step 2.2: Recombination

/*Generate a trial vector $U_{i,G} = \{u_{i,G}^1, \dots, u_{i,G}^D\}$ for each target vector $X_{i,G}$ */

FOR i=1 to NP

$J_{rand} = \lfloor \text{rand} [0,1) * D \rfloor$

FOR j =1 to D

$$u_{i,G}^j = \begin{cases} v_{i,G}^j & \text{if } (\text{rand} [0,1) \leq CR) \text{ or } (j = j_{rand}) \\ x_{i,G}^j & \text{otherwise} \end{cases}$$

END FOR

Step 2.3: Selection

/* Selection*/

FOR i =1 to NP

Evaluate the trial vector $U_{i,G}$

IF $f(U_{i,G}) \leq f(X_{i,G})$

, THEN $X_{best,G} = U_{i,G}$

, $f(X_{i,G+1}) = f(U_{i,G})$

IF $f(U_{i,G}) < f(X_{best,G})$

, THEN $X_{best,G} = U_{i,G}$

, $f(X_{best,G}) = f(U_{i,G})$

END IF

END IF

END FOR

Step 2.4: Increment the generation count

$G=G+1$

Step 3: END WHILE

Mutation operation. Each of the N parameter vectors undergoes mutation, recombination, and selection. Mutation expands the search space. For a given parameter vector $X_{i,G}$, randomly select three vectors $X_{1,G}, X_{2,G}, \dots, X_{3,G}$, such that the indices $1, r1, r2, r3$ are distinct. Add the weighted difference of two of the vectors to the third $V_{i,G} = X_{r1,G} + F(X_{r2,G} - X_{r3,G})$. The mutation factor F is a constant from $[0,2]$. $V_{i,G}$ is called the donor vector.

Recombination operation. Recombination incorporates successful solutions from the previous generation. The trial vector $U_{i,G+1}$ is developed from the elements of the target vector, $X_{i,G}$, and the elements of the donor vector, $V_{i,G+1}$. Elements of the donor vector enter the trial vector with probability CR .

$$U_{j,i,G+1} = \begin{cases} V_{j,i,G+1} & \text{if } rand_{j,i} \leq CR \text{ or } j = I_{rand} \\ X_{j,i,G} & \text{if } rand_{j,i} > CR \text{ or } j \neq I_{rand} \end{cases}$$

$rand_{j,i} \sim U[0,1]$, I_{rand} is a random integer from $[1,2,\dots,D]$. I_{rand} ensuring that $V_{i,G+1} \neq X_{i,G}$.

Selection operation. The target vector $X_{i,G}$, is compared with the trial vector $V_{j,i,G+1}$ and the one with the lowest function value is admitted to the next generation.

$$X_{i,G+1} = \begin{cases} U_{i,G+1} & \text{if } f(U_{i,G+1}) \leq f(X_{i,G}) \\ X_{i,G} & \text{otherwise} \end{cases}$$

Mutation, recombination, and selection continue until some stopping criterion is reached; in the example, $NP=100$; F is 2; and CR is 0.8. Distances are given in Table 1.

Particle swarm optimization algorithm

Eberhart and Kennedy (1995) developed a novel optimization algorithm named particle swarm optimization that mimicked the flying behavior of a flock of birds; the algorithm has been verified as efficient for solving both continuous and discrete optimization problems (Figure 2).

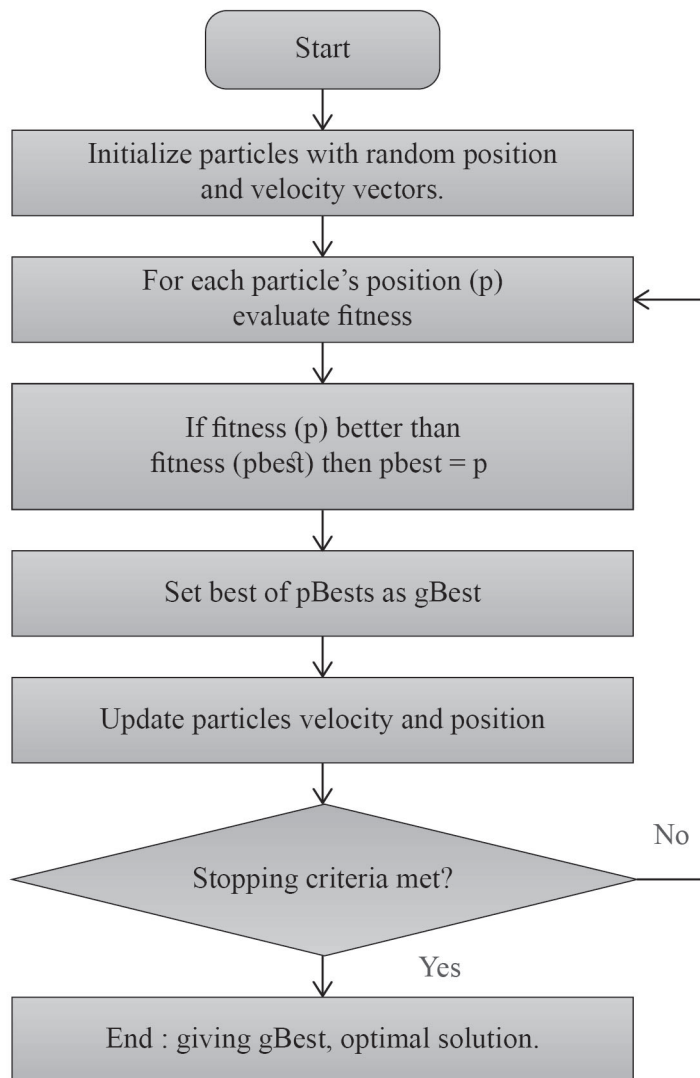


Figure 2. Flowchart of particle swarm optimization algorithm.

The structure of the particle swarm optimization algorithm is as follows:

Notation:

c_p	: the particle best acceleration constant
c_g	: the global best acceleration constant
w	: the inertia weight
r	: uniform random number in range [0,1]
x_i	: the position vector of particle i
v_i	: the velocity vector of particle i
$pBest_i$	: the personal best of the particle i
$gBest$	: the global best

Procedure: Particle swarm optimization.

Input: $f(x)$, $v_i(0)$, $pbest_i(0)$, $gbest_i(0)$, c_p , c_g

Output: Best solution

begin

$t = 0$

Step 1: initialize $x_i(t)$;

Step 2: evaluate $x_i(t)$;

while (not terminating condition) do

for each particle x_i in swarm do

Step 3: $v_i(t+1) = w(t)v_i(t) + c_p r(pbest_i - x_i(t)) + c_g r(gbest_i - x_i(t))$;

Step 4: $x_i(t+1) = x_i(t) + v_i(t+1)$; //

Step 5: evaluate $x_k(t)$;

if $f(x_i(t+1)) \leq f(pbest_i(t+1))$;

Step 6: update $pbest_i(t+1) \leq x_i(t+1)$;

end;

Step 7: $gbest_i(t+1) = \operatorname{argmin}\{f(pbest_i(t+1)), f(pbest_i(t+1))\}$

$t = t + 1$

end;

output: the best solution gbest;

end.

Hybrid differential evolution and particle swarm optimization

Pant et al. (2008) developed the hybrid DEPSO algorithm to solve continuous optimization problems, helping to maintain population diversity and producing a good optimal solution. All algorithms used the same encoding-decoding algorithm.

The encode method. The operation vectors show each candidate solution for the flexible flow shop scheduling with tooling constraints problem. Encoding of each vector is randomly numbered from 0 to 1 as a real number. According to the size of the population considered, each vector has a dimension value equal to the number of fields considered, as shown in Figure 3.

Vector/Particle	Field1	Field2	Field3	Field4	Field5
1	0.36	0.67	0.27	0.69	0.34
2	0.21	0.99	0.10	0.68	0.90
3	0.05	0.95	0.86	0.81	0.33
4	0.82	0.06	0.25	0.19	0.90
5	0.12	0.26	0.34	0.60	0.59

Figure 3. Operation-based encoding.

The pseudo code of the hybrid DEPSO Algorithm is:

Notation:

G : Generation number
 P_G : Population of NP-D-dimension
 $X_{i,G}$: Random vector
 $V_{i,G}$: Mutant vector
 $U_{i,G}$: Trial vector
 D : Dimensional parameter
 $\text{randb}(j)$: A random number generated from $[0,1]$
 $\text{rnbr}(i)$: A random integer from $[1,2,\dots,D]$
 J_{rand} : Position vector of particle i
 F : Scaling factor
 cp : Particle best acceleration constant
 cg : The global best acceleration constant
 w : Inertia weight
 r : Uniformly random number in range $[0,1]$
 xi : Position vector of particle i
 vi : Velocity vector of particle i
 $pBest_i$: Personal best of the particle i
 $gBest$: Global best

Step 1: Set the generation number $G = 0$, $P_G = \{X_{1,G}, \dots, X_{NP}\}$ with $X_{i,G} = \{x_{i,G}^1, \dots, x_{i,G}^D\}$, $i = 1, \dots, NP$, uniformly distributed in the range $[X_{\min}, X_{\max}]$, where $X_{\min} = \{x_{\min}^1, \dots, x_{\min}^D\}$ and $X_{\max} = \{x_{\max}^1, \dots, x_{\max}^D\}$.

Step 2: WHILE stopping criterion is not satisfied, DO

Step 2.1: Mutation

/*Generate a mutated vector $V_{i,G} = \{v_{i,G}^1, \dots, v_{i,G}^D\}$ for each target vector $X_{i,G}$ */

FOR $i=1$ to NP

Generate a mutated vector $V_{i,G} = \{v_{i,G}^1, \dots, v_{i,G}^D\}$ corresponding to the target vector $X_{i,G}$

END FOR

Step 2.2: Recombination

/*Generate a trial vector $U_{i,G} = \{u_{i,G}^1, \dots, u_{i,G}^D\}$ for each target vector $X_{i,G}$ */

FOR $i=1$ to NP

$J_{\text{rand}} = \lfloor \text{rand}[0,1) * D \rfloor$

For $j=1$ to D

$$u_{i,G}^j = \begin{cases} v_{i,G}^j & \text{if } (\text{rand}[0,1) \leq CR) \text{ or } (j = j_{\text{rand}}) \\ x_{i,G}^j & \text{otherwise} \end{cases}$$

END FOR

Step 2.3: Selection

```

/* Selection*/
FOR i =1 to NP
    Evaluate the trial vector  $U_{i,G}$ 
    IF  $f(U_{i,G}) \leq f(X_{i,G})$  , THEN  $X_{best,G} = U_{i,G}$ 
        ,  $f(X_{i,G+1}) = f(U_{i,G})$ 
    Else
        PSO activated. Find a new particle
         $v_i(t+1) = w(t)v_i(t) + c_p r(pbest_i - x_i(t)) + c_g r(gbest_i - x_i(t))$ 
         $x_i(t+1) = x_i(t) + v_i(t+1)$ 

        Evaluate  $f(PSO_{U_{i,G}}) = x_k(t)$ ;
        IF ( $f(PSO_{U_{i,G}}) \leq f(X_{i,G})$ )
            ,  $f(X_{i,G+1}) = f(PSO_{U_{i,G}})$ 
        Else
             $X_{i,G+1} = X_{i,G}$ 
        End IF
    End FOR

```

The decode method. Decoding sorts the rank order value of each vector in ascending order. The vectors will assign the sequence of operations of the machine. The next step is the allocation of fields to machines. Fields will be allocated randomly to the machines at each stage by following the sequence of operations in the rank order value steps. For example, the assignment of five fields on a two-stage production system with two machines in each stage is sequenced as follows: *field 3 - field 5 - field 1 - field 2 - field 4*, as shown in Figure 4.

Vector/Particle	Field1	Field2	Field3	Field4	Field5
	0.36	0.67	0.27	0.69	0.34

Vector/Particle (ROV)	Field3	Field5	Field1	Field2	Field4
	0.27	0.34	0.36	0.67	0.69

Figure 4. An example of decoding performed by sorting the rank order value.

After the random vectors/particles are sorted, the field sequence and machine assignment for each field must be assigned. Then, changing setup tool time and machine eligibility can be assigned simultaneously for calculating the completion time. Random machines are assigned to fields that minimize completion time. Moreover, fields are assigned to the machine that minimizes the completion time, as shown in Figure 5.

Stage1	M1	J3	J1	J4	
	M2	J5	J2		
Stage2	M1		J3	J1	J4
	M2		J5	J2	

Figure 5. Decoding the particle to active scheduling.

Computational experiments

In this section, several computational experiments are reported from various test problems. The case has been established based on the number of fields (n), number of stages (s), and number of machines (m). Each case can be identified in the form of “Number of stage × Number of machines in each stage × Number of products”. For instance, a problem with six stages, two machines at the first stage, two machines at the second stage, three machines at the third stage, two machines at the fourth stage, two machines at the fifth stage, and two machines at the sixth stage with 10 fields can be denoted by “6 x (2-2-3-2-2-2) x 10”. Consider the makespan with six stages to be processed on three types of tractors with six types of tools. The processing times, tool change times of types 1, 4, 5, and 6 and tool change times of types 2 and 3 are shown in Tables 1, 2, and 3. The experiments run for 10 replications.

Table 1. Data used in the experiments.

Data	Tractor type		
	Type 1	Type 2	Type 3
Processing time (min/ton)	10	15	15

Table 2. Data used in tool change time of types 1, 4, 5, and 6.

Tool type	1	4	5	6
1	0	30	30	30
4	30	0	30	30
5	30	30	0	30
6	30	30	30	0

Table 3. Data used in tool change time of types 2 and 3.

Tool type	2	3
2	0	40
3	40	0

Pilot experiments were performed to test a set of potential values for each parameter to find the appropriate differential evolution algorithm and particle swarm optimization parameters. The parameter values used in this paper are presented in Tables 4, 5, and 6.

Table 4. Parameter values for the differential evolution algorithm.

Parameter	Value
Population number (NP)	50
Maximum iterations (T)	100
Mutation factor (F)	1
Crossover constant (CR)	0.8

Table 5. Parameter values for the particle swarm optimization algorithm.

Parameter	Value
Population size (K)	50
Maximum iterations (T)	100
Personal best position acceleration constant	cp = 0.5
Global best position acceleration constant	cg = 0.75
Inertia weight	w(t) = 0.9

Table 6. Parameter values for the hybrid DEPSO algorithm.

Parameter	Value
Maximum iterations (T)	100
Population number (NP)	50
Mutation factor (F)	1
Crossover constant (CR)	0.8
Population size (K)	50
Personal best position acceleration constant	cp = 0.5
Global best position acceleration constant	cg = 0.75
Inertia weight	w(t) = 0.9

RESULTS

This section compares findings from the differential evolution algorithm, particle swarm optimization, and hybrid DEPSO algorithms that were created with 10 different problem sets: Set 1 – $6 \times (3-2-2-3-3-3) \times 10$; Set 2 – $6 \times (4-2-2-4-4-4) \times 10$; Set 3 – $6 \times (4-2-2-4-4-4) \times 20$; Set 4 – $6 \times (4-2-2-4-4-4) \times 20$; Set 5 – $6 \times (5-2-2-5-5-5) \times 30$; Set 6 – $6 \times (5-3-3-5-5-5) \times 30$; Set 7 – $6 \times (5-3-3-5-5-5) \times 40$; Set 8 – $6 \times (6-2-2-6-6-6) \times 40$; Set 9 – $6 \times (6-3-3-6-6-6) \times 50$; Set 10 – $6 \times (7-3-3-7-7-7) \times 50$. The computational results with the averages and the best solution obtained by the proposed algorithms are presented in Table 7; the hybrid DEPSO had a better makespan solution than the differential evolution algorithm and particle swarm optimization for eight of the problems. The hybrid method demonstrated an outstanding ability to solve flexible flow shop problems. The relative improvement results showed that the differential

evolution algorithm, particle swarm optimization, and hybrid DEPSO algorithms improved the makespan solution by averages of 8.98%, 8.44%, and 9.96%, respectively (Table 8). While the hybrid DEPSO gave the best solution, its computational time was relatively high (Table 7, Figure 6), although at an acceptable level.

To measure the quality of makespan solution generated by the proposed algorithms, the relative improvement of the makespan solutions obtained by the current practice algorithm with respect to those of the differential evolution algorithm, particle swarm optimization, and hybrid DEPSO algorithms were calculated using equation (1). All algorithms were developed using MATLAB software, version 7.7.0.471 (R2008b) on Intel® Core(TM) i7-6700HQ CPU @ 2.80 GHz RAM (8 GB RAM).

Where,

RI = the relative improvement (%) between sol_current and sol_metaheuristic,

$$RI (\%) = \frac{Sol_{current} - Sol_{metaheu}}{Sol_{current}} \quad (1)$$

$Sol_{current}$ = the solution obtained from the current practice, and

$Sol_{metaheu}$ = the solution obtained from the differential evolution algorithm, particle swarm optimization or hybrid DEPSO algorithm

Table 7. Solution quality in terms of the objective function.

Problem	Size			Makespan (hr)			Computation time (sec)			
	Stages	Machine	Fields	Current practice	Average			Average		
					DE	PSO	Hybrid	DE	PSO	Hybrid
1	6	(3-2-2-3-3-3)	10	26.13	19.40	19.40	19.40	7.31	7.98	14.24
2	6	(4-2-2-4-4-4)	10	18.33	16.00	16.00	16.00	7.08	9.58	15.46
3	6	(4-2-2-4-4-4)	20	44.33	39.50	40.83	39.25	162.14	179.23	267.58
4	6	(4-2-2-4-4-4)	20	39.50	35.83	35.83	35.33	200.66	223.6	489.785
5	6	(5-2-2-5-5-5)	30	55.83	51.75	52.33	50.83	374.34	390.97	600.12
6	6	(5-3-3-5-5-5)	30	62.63	59.67	60.00	58.20	415.22	433.08	797.81
7	6	(5-3-3-5-5-5)	40	97.37	90.58	90.83	89.57	396.84	413.51	823.78
8	6	(6-2-2-6-6-6)	40	103.50	99.33	99.50	97.33	532.56	543.56	1076.63
9	6	(6-3-3-6-6-6)	50	111.18	106.25	106.83	105.92	562.34	563.9	1207.06
10	6	(7-3-3-7-7-7)	50	114.17	109.83	110.00	109.17	645.69	660.88	1341.94

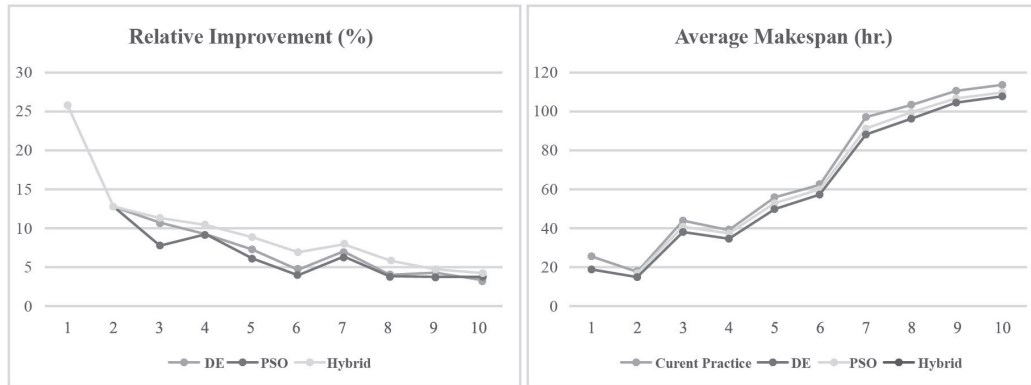


Figure 6. Percentage relative improvement and makespan for each test problem.

Table 8. Percentage relative improvements for each algorithm.

Problem	Size			RI (%)		
	Stages	Machine	Fields	DE	PSO	Hybrid
1	6	(3-2-2-3-3-3)	10	25.77	25.77	25.77
2	6	(4-2-2-4-4-4)	10	12.73	12.73	12.73
3	6	(4-2-2-4-4-4)	20	10.90	7.89	11.47
4	6	(4-2-2-4-4-4)	20	9.28	9.28	10.55
5	6	(5-2-2-5-5-5)	30	7.31	6.27	8.96
6	6	(5-3-3-5-5-5)	30	4.74	4.20	7.08
7	6	(5-3-3-5-5-5)	40	6.97	6.71	8.01
8	6	(6-2-2-6-6-6)	40	4.03	3.86	5.96
9	6	(6-3-3-6-6-6)	50	4.44	3.91	4.74
10	6	(7-3-3-7-7-7)	50	3.65	3.80	4.38
Average				8.98	8.44	9.96

DISCUSSION

The sugarcane cultivation process is very complicated. We addressed the limitations of sugarcane cultivation, such as tooling constraints (setup time was considered as tool changing time only) and machine eligibility. An efficient scheduling method is an important problem in academic and industrial research.

In scheduling flexible flow shop problems, Baumann and Trautmann (2011) developed mixed integer programming for minimizing changeover times, but this method can only solve small problems. Chamnanlor and Sethanan (2015), Chamnanlor et al. (2017), and Sangsawang et al. (2015) developed hybrid particle swarm optimization with a Cauchy distribution for the optimal sequencing of problems involving a reentrant hybrid flow shop scheduling problem with time window for minimizing makespan. Batur et al. (2016) used a simulated annealing

based heuristic for scheduling problems arising in hybrid flexible flow shop problems that repeatedly produce a set of multiple part types. Although most tooling constraint studies have looked at different problems, they have similar objectives, such as minimizing makespan or minimizing completion time (Melnik et al. (1989), Widmer (1991), Widmer (1991), Ghosh et al. (1992), Gultekin et al. (2006), Chen (2008), Zeballos (2010), Zeballos et al. (2010), Xu et al. (2013)). This study found that the differential evolution algorithm, particle swarm optimization and hybrid DEPSO were effective and could allocate resources for sugarcane cultivation scheduling: all algorithms found better solutions than the current practice. Our performance comparison between the differential evolution algorithm and particle swarm optimization showed that the differential evolution algorithm performed better than particle swarm optimization in terms of quality, resolution and computation time, while hybrid DEPSO algorithms provided better answers than the differential evolution algorithm and the particle swarm optimization algorithm, which took more time to compute. The superiority of hybrid DEPSO over the differential evolution algorithm and particle swarm optimization has also been demonstrated in other research fields, such as flexible flow shop scheduling (Chamnanlor et al. (2017), Sangsawang et al. (2015), Batur et al. (2016)) and hybrid DEPSO algorithms (Jayabarathi et al. (2007), Li et al. (2008), Li et al. (2014)).

As sugarcane cultivation has only six steps, other cultivation systems may not be able to apply this research directly. Our solution is suitable for smallholder farmers that either do not own their own equipment or with insufficient tractors and tools to improve the soil for growing sugarcane.

CONCLUSION

This paper has presented the implementation of a particle swarm optimization algorithm and a differential evolution algorithm for optimizing multistage flexible flow shop scheduling problems in the sugar industry with dependent tooling constraints and machine eligibility constraints. The objective is to minimize the makespan. A differential evolution algorithm, a particle swarm optimization algorithm and a hybrid DEPSO algorithm were developed to solve practical problems. The differential evolution algorithm and the particle swarm optimization algorithm were compared to evaluate the effectiveness of the heuristics algorithm from real-world cases of planting sugarcane. This paper showed that the differential evolution algorithm gave an RI of makespan of 8.98%, the particle swarm optimization algorithm gives a RI of makespan of 8.44% and the hybrid DEPSO algorithm gives a RI of makespan of 9.96%.

Although the hybrid DEPSO algorithm demonstrated an outstanding ability to solve the problem, it is possible to modify the differential evolution algorithm or the particle swarm optimization algorithm and use other meta-heuristics or hybrid methods to improve solutions. All three methods could minimize the makespan. The hybrid DEPSO algorithm gave the best answer by reducing the time to complete the work by 9.96% relative to current practice. Future research should consider the start time of machines for cultivation and include the distance between field i and field j for each cultivation process. The approach applied in this study can extended to other other agricultural industries.

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